

Towards Model Reduction for Power System Transients with Physics-Informed Neural PDE

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The Fifth Autonomous Energy Systems Workshop

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- L. Pagnier, J. Fritzsich, P. Jacquod and M. Chertkov, "Toward Model Reduction for Power System Transients With Physics-Informed PDE", in IEEE Access, vol. 10, pp. 65118-65125, 2022, doi: 10.1109/ACCESS.2022.3183336.



Laurent Pagnier



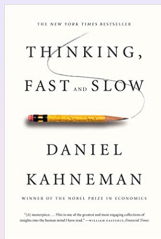
Julian Fritzsich



Philippe Jacquod

Outline

- 1 System 1 & System 2 ML for Power Systems
 - Modern Applied Mathematics as System 2
 - Machine Learning for Power Systems
- 2 Power System Transients With Physics-Informed PDE
 - PIML for State & Parameter Estimation
 - Model Reduction
 - From ODEs to PDEs in Power Systems
 - Summary & Path Forward

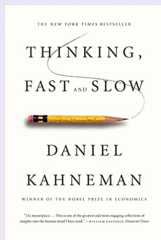


System 1 & 2 in Deep Learning & AI

- "From System 1 Deep Learning to System 2 Deep Learning" – Yoshua Bengio, NeurIPS 2019
- "Combining Fast and Slow Thinking for Human-like and Efficient Navigation in Constrained Environments" – M. Ganappini, et al, arXiv:2201.07050

● System 1 – operates automatically & quickly

● System 2 – allocates attention to effortful mental activities

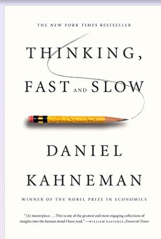


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 - **Deep Learning** empowered by **Automatic Differentiation**

- System 2 – allocates attention to effortful mental activities
 - **Physics Informed Machine Learning** – more generally **Explainable Heuristics in Quantitative Sciences**



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- **Deep Learning** empowered by **Automatic Differentiation**

- System 1.5

- 20th century Applied Math – ODE, PDE, **Sensitivity Analysis**

- System 2 – allocates attention to effortfull mental activities

- **Physics Informed Machine Learning** – more generally **Explainable Heuristics in Quantitative Sciences**

Physics Informed Machine Learning for Power Systems

Machine Learning (e.g. Neural Network, Graph Models, etc)

- will make Power System Computations
 - faster (efficient)
 - possible even when data/measurements incomplete
- requires ground-truth data
 - actual measurements (Phasor Measurement Units, etc)
 - power flow solvers (microscopic simulations) – reliable, possibly heavy
- can be power-system "informed" (System 2) vs "agnostic" (System 1)
 - What is System 1 today may become System 2 tomorrow (with proper theory & enough of experiments)
- methods/options are many
 - should be gauged to available data, level of uncertainty, etc

Incomplete Review: Brief, Recent, Biased AI/ML in Power Systems (System 1, System 2 & juxtaposition)

- Structure Learning, Sparse Measurements, Graphical Models, Focus on Power Distribution: Deka, et al [2016-2019]
- Learning ODE: Power Transmission, Dynamic Coefficients in Swing Equations, Deterministic and Stochastic, Lokhov, et al [2017]
- Real-time Faulted Line Localization and PMU Placement in Power Transmission through CNN: Li, et al [2018]
- Collocation Point Neural ODE for Power Systems: Misuris, et al [2018]
- Learning a Generator Model from Terminal Bus Data: many ML schemes, tradeoffs, ranking models according to regimes, Stulov et al [2019]
- Learning from power system data stream, phasor-detective approach, Escobar et al [2019]

Incomplete Review: Brief, Recent, Biased

AI/ML in Power Systems (System 1, System 2 & juxtaposition)

- **Physics-Informed** Graphical Neural Network for **Parameter & State Estimations** in Power Systems
<https://arxiv.org/abs/2102.06349> (Pagnier & MC))
- **Embedding Power Flow** into Machine Learning for Parameter and State Estimation <https://arxiv.org/abs/2103.14251> (Pagnier & MC)
- **Which Neural Network to Choose** for Post-Fault Localization, Dynamic State Estimation and Optimal Measurement Placement in Power Systems? <https://arxiv.org/abs/2104.03115> (Afonin & MC))

Machine Learning (Neural Networks) Setting

NN models: General

- $NN_{\vec{\phi}}(\vec{x}) = \vec{y}$
 - Vector, $\vec{\phi}$, of Not-Interpretable Parameters
 - Input vector: \vec{x}
 - Output vector: \vec{y}

NN models: Loss Functions

- L2 norm $\|\dots\|$
- Probabilistic (Cross Entropy or Kullback-Leibler)
- Regularizations, e.g. L1 (sparsity, physical, etc)

NN models: Architectures

- **Convolutional NN** (LeCun 1989 –)
- **Graph NN** (Scarcelli. et al 2009 –)
- **Neural ODE** (Chen et al 2008 –)
- **Collocation Point NN** (Lagaris et al 1998, Raissi et al 2019 –)
- **Hamiltonian NN** (Greydanus et al 2018 –)

Power Flow Equations

- grid-graph, $\mathcal{G} = (\mathcal{V}, \mathcal{E})$
- complex-valued powers: $\forall a \in \mathcal{V} : S_a \equiv p_a + iq_a$
- complex-valued (electric) potentials, $\forall a \in \mathcal{V} : V_a \equiv v_a \exp(i\theta_a)$,
- Power Flow (PF) equations:

$$p_a = \sum_{b; \{a,b\} \in \mathcal{E}} v_a v_b \left[g_{ab} \cos(\theta_a - \theta_b) + \beta_{ab} \sin(\theta_a - \theta_b) \right],$$

$$q_a = \sum_{b; \{a,b\} \in \mathcal{E}} v_a v_b \left[g_{ab} \sin(\theta_a - \theta_b) - \beta_{ab} \cos(\theta_a - \theta_b) \right],$$

- Direct PF Map: $\Pi_{\mathcal{V}} : \mathbf{S} \equiv (S_a | a \in \mathcal{V}) \mapsto \mathbf{V} \equiv (V_a | a \in \mathcal{V})$ - implicit (need to solve eqs. - System 1 & System 2 ML may be useful <https://arxiv.org/abs/2103.14251> L. Pagnier & MC)

Task: State & Parameter Estimation

- Inverse PF Map: $\mathbf{S} = \mathbf{\Pi}_Y^{-1}(\mathbf{V})$ – explicit (do not need to solve eqs. – System 1 and System 2 ML may be useful
<https://arxiv.org/abs/2102.06349> L. Pagnier and MC)

- State Estimation

- Full Observability: given \mathcal{G} and \mathbf{Y} to estimate injected/consumed active and reactive powers = application of the inverse PF map, $\mathbf{\Pi}^{-1}$
- Limited Observability:
 - Complement Missing power injections/consumptions at the nodes where voltages and phases are measured
 - Challenging Version: to reconstruct injected/consumed powers and also voltages and phases at all nodes of the system. (super-resolution – will not discuss)

- Parameter Estimation

- Reconstruct Graph, $\mathcal{G} = (\mathcal{V}, \mathcal{E})$, and line characteristics, \mathbf{Y}

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How does model reduction work?

- **Ground Truth** – reliable but computations "heavy"
- \Rightarrow
- **Reduced Model** – lighter computations-wise, losing some accuracy (but hopefully not too much)

Transient (seconds) Dynamics of the grid

- **Swing Equation**: $m_i \ddot{\theta}_i + d_i \dot{\theta}_i = p_i - \sum_j v_i v_j b_{ij} (\theta_i - \theta_j)$
- **Reduced Model** Options?

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PDE as the **Reduced Model**

- $$m(\mathbf{r}) \frac{\partial^2}{\partial t^2} \theta(t; \mathbf{r}) + d(\mathbf{r}) \frac{\partial}{\partial t} \theta(t; \mathbf{r}) = p(t; \mathbf{r}) + \sum_{\alpha, \beta=1,2} \partial_{r_\alpha} b_{\alpha\beta}(\mathbf{r}) \partial_{r_\beta} \theta(t; \mathbf{r})$$

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- Why is **Partial Differential Equation** modeling a sound option for model reduction?

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Approximating the swing ODEs by a PDE? Really?

- Naively: increases # degrees of freedom

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... but thinking a bit more (system 2):

- It has a sense because
 - Solutions of linear 2+1 dimensional PDE assume spatial regularization via a 2d grid with fewer # grid points
 - Operations are much more efficient over a regular grid
 - # physical parameters can be reduced dramatically via coarsening – fewer & large-scale harmonics

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Inspired by – 1+1 PDE modeling of PS:

- A. Semlyen, 1974.
- J. S. Thorp, C. E. Seyler, and A. G. Phadke, 1998.
- M. Parashar, J. S. Thorp, and C. E. Seyler, 2004.

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How can we make it work?

- In the Core of **This Talk** !

From Swing Model to PDE Model

- From Swing Equation: $m_i \ddot{\theta}_i + d_i \dot{\theta}_i = p_i - \sum_j v_i v_j b_{ij} (\theta_i - \theta_j)$
- To PDE as the Reduced Model

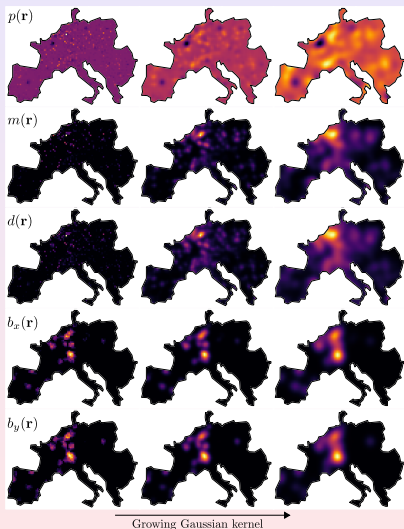
$$m(\mathbf{r}) \frac{\partial^2 \theta(t; \mathbf{r})}{\partial t^2} + d(\mathbf{r}) \frac{\partial \theta(t; \mathbf{r})}{\partial t} = p(t; \mathbf{r}) + \sum_{\alpha, \beta=1,2} \partial_{r_\alpha} b_{\alpha\beta}(\mathbf{r}) \partial_{r_\beta} \theta(t; \mathbf{r})$$
- $\forall i: \theta_i(t) \rightarrow \theta(t; \mathbf{r}), m_i \rightarrow m(\mathbf{r}), d_i \rightarrow d(\mathbf{r}), p_i(t) \rightarrow p(t; \mathbf{r}), b_{ij} \rightarrow b_{\alpha\beta}(\mathbf{r}), \forall \alpha, \beta = 1, 2.$

Neumann Boundary Conditions:

- Vanishing normal derivative of the angle field on the domain boundary $\partial\Omega$:

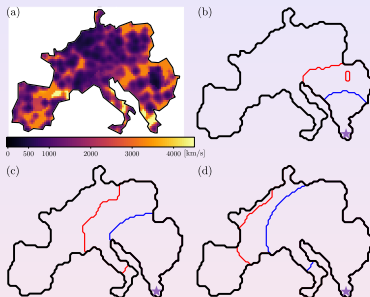
$$\forall t, \forall \mathbf{r} \in \partial\Omega: \sum_{\alpha, \beta=1,2} n_\alpha(\mathbf{r}) b_{\alpha\beta}(\mathbf{r}) \partial_{r_\beta} \theta(t; \mathbf{r}) = 0$$
- e.g. guaranteeing equilibration to the same frequency

Initialization Parameters: Artificial Diffusion & Calibration



- Artificial Diffusion (AD) – "diffusive growth" of non-uniform distribution of parameters
- Generalization of the methodology developed in M. Parashar, J. S. Thorp, and C. E. Seyler (2004) for 1+1 PDEs
- AD is stopped when parameters satisfy some smoothness criterion – advantageous because it allows the optimal width of the Gaussian kernel to be self-determined

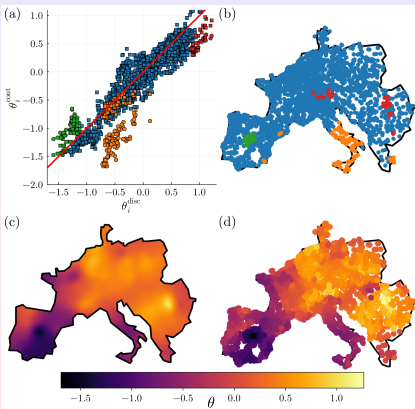
Speed of EM waves: Inhomogeneous Map



- PanTaGruEl model: 3809 buses, 618 generators and 4944 lines. (3221 nodes in the "full" discretization of our PDE model.)

- (a) Assessment of the local propagation speed as $c(\mathbf{r}) = \sqrt{b(\mathbf{r})/m(\mathbf{r})}$.
- (b)-(d) Fronts of the perturbation at incremental time intervals of $\Delta t = 0.6s$, after a fault in Greece (violet star), for inhomogeneous (red) and average parameters (blue) – slower.

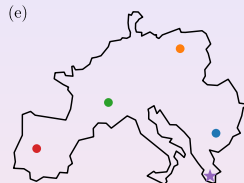
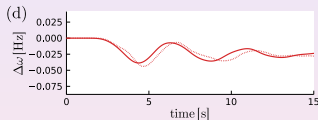
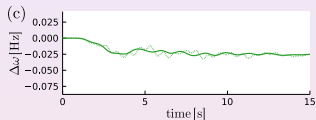
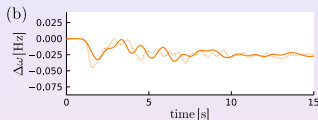
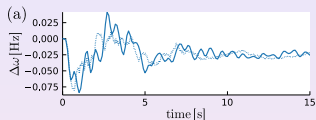
Steady State Test & Adjustments



- (a) One-to-one comparison of local voltage angle: for each bus in the discrete model the nearest node in the continuous mesh is selected. The red line indicates a perfect match.
- (b) The outliers marked in orange, red and green correspond to the points marked on the map in (b). The square markers correspond the solution after adjusting the susceptances.
- (c) PDE solution $\theta(\mathbf{r})$ after adjustment.
- (d) GT (ODEs) solution θ^{disc} .

Steady State: PDE vs Ground Truth (ODE)

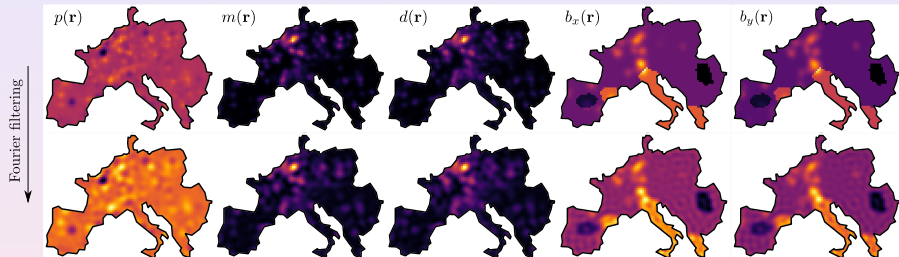
Frequency Response of Generators



PDE vs Ground Truth (ODE)

- Response in (a) Bulgaria, (b) Poland, (c) France, and (d) Spain to a 900 MW loss of power in Greece.
- dotted – PDE, solid – Ground Truth (ODEs)

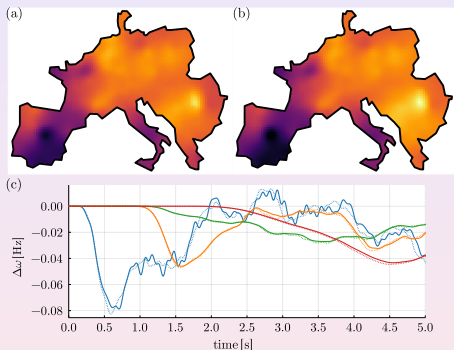
Coarse-Graining/Filtering



Distribution of the grid parameters: Low-Pass Filtering

- Original vs a Fourier Low-Pass Filter with a cut-off frequency 30% (of the maximum).

Coarse-Graining/Filtering



- (a) – original vs (b) – filtered: Comparison of Steady state solution
- (c) Frequency response original (solid) vs filtered (dotted)

30% of filtering – almost no loss accuracy

What did we achieve so far?

- **Construction** of the **reduced** PDE model (of the ODE/swing equations). Included:
 - 1 accurate resolution of the **boundary conditions**
 - 2 efficient and flexible identification of parameters based on **Artificial Diffusion** and **Fourier Filtering**
- **Validation** via **Static** and **Dynamic** Tests – reduced PDE vs Ground Truth (ODEs)
- **Observation:** — PDE offers significant **gain in efficiency**:
 - 1 Evaluation of PDE is faster at least factor of ten (for the same number of discretization points)
 - 2 Can run PDE at much lower resolution
 - 3 Can use much fewer degrees of freedom \Rightarrow **to learn**

Work in Progress: Towards Physics (System 2) Informed ML

- Functional maps for $m(\mathbf{r})$, $d(\mathbf{r})$ and $b_{\alpha\beta}(\mathbf{r})$ will be modeled as Neural Networks (System 1)
- Artificial Diffusion (AD) for the warm start

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Goal — efficient & accurate evaluation of multiple scenarios

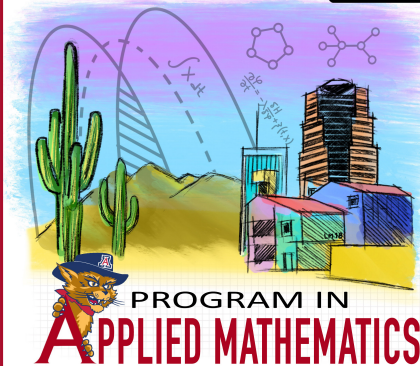
- Automatic & much faster than an individual Dynamic Simulation of today (also faster than real dynamics)

- Research focused, since 1976, one of the US first [dynamical systems, integrability, turbulence ...]
- **Interdisciplinary**: 100+ professors/ 26 departments/ 8 colleges **across UA** campus (CoS & CoE & Optics – top 3)
- Mixing traditional @ **contemporary** Applied Math
- **Graduate**, Ph.D. focused, no terminal M.Sc.
- 60 Ph.D students (**13/16/10** enrolled in **2021/2019**)
- **3 Core Courses** (1st year -- Methods, Analysis, Algorithms)
<https://appliedmath.arizona.edu/students/new-core-courses>
- Strong collaborations with **Industry** (e.g. Raytheon, Uber, Intel, Critical Path, etc) and **National Labs** (e.g. LANL, LLNL, NREL, NNSS, etc)
- **5 seminar/colloquium series** – recorded and posted online
- Participation in many UA & National **Edu Projects**

<http://appliedmath.arizona.edu/>

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SCAN ME





Support is Appreciated !!

- **Energy Systems:**
UArizona start up +
DOE/ARPA-E

Thanks for your attention !

Outline

3 Neural State and Parameter Estimations: Details

Task SE & PE. Reduced Modeling.

- Setting of Partial Observability
- Find Equivalent (Reduced) Model of Power System
- "Inspired" by Kron Reduction
 - $I^{(o)} = \mathbf{Y}^{(r)} \mathbf{V}^{(o)}$
 - "o" - observed; "r" - reduced
 - $\mathcal{G}^{(r)} \equiv (\mathcal{V}^{(o)}, \mathcal{E}^{(r)})$
 - $\mathbf{Y}^{(r)} \doteq (\{a, b\} | Y_{ab}^{(r)} \neq 0)$ – associated with the effective (not necessarily real) power lines, $\{a, b\} \in \mathcal{E}^{(r)}$. $\mathbf{Y}^{(r)}$
- Reduced Model
 - $\mathbf{S}^{(o)} = \mathbf{\Pi}_{\mathbf{Y}^{(r)}}^{-1}(\mathbf{V}^{(o)})$
 - Learn it !?

Task: SE & PE. PIML of Reduced Model

- Power Graphical NN (System 2):

$$\min_{\varphi, \mathbf{Y}^{(r)}} L_{\text{Power-GNN}} \left(\varphi, \mathbf{Y}^{(r)} \right),$$

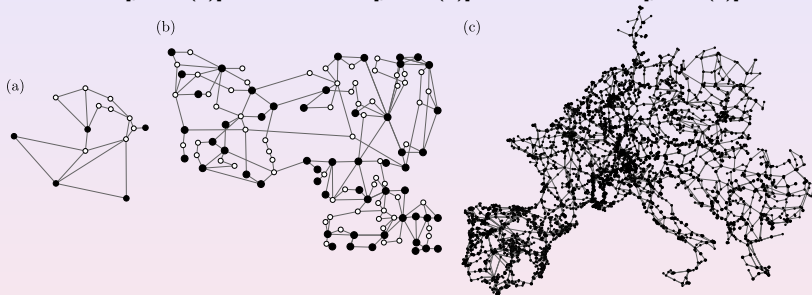
$$L_{\text{Power-GNN}} \left(\varphi, \mathbf{Y}^{(r)} \right) \equiv \frac{1}{N|\mathcal{V}^{(o)}|} \sum_{n=1}^N \left\| \mathbf{S}_n^{(o)} - \underbrace{\Pi_{\mathbf{Y}^{(r)}}^{-1} \left(\mathbf{V}_n^{(o)} \right)}_{\text{physics = interpretable}} - \underbrace{\Sigma_{\varphi} \left(\mathcal{V}_n^{(o)}, S_n^{(o)} \right)}_{\text{NN = "sub-scale"}} \right\|^2 + \underbrace{\mathcal{R}(\varphi)}_{\text{regularization}}$$

- SIMULTANEOUSLY physics-informed and physics-blind parts
- Compare with Vanilla-NN (System 1)

$$L_{\text{NN}} \doteq \frac{1}{N|\mathcal{V}^{(o)}|} \sum_{n=1}^N \left\| \mathbf{S}_n^{(o)} - \text{NN}_{\varphi} \left(\mathbf{V}_n^{(o)} \right) \right\|^2$$

Task: SE & PE. Power GNN vs Vanilla NN. Experiments.

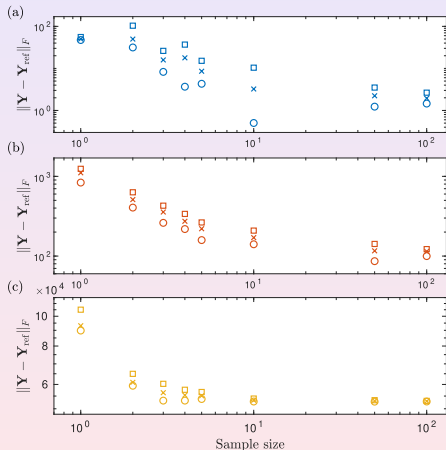
IEEE 14-bus [panel (a)], IEEE 118-bus [panel (b)] and PanTaGruEl [panel (c)] models



State Estimation Test: Six set of samples were generated for each network. Average mismatch of predicted power injections (on the training set in parenthesis)

	case #1	case #2	case #3	case #4	case #5	case #6
Vanilla NN	4.9E-6 (4.2E-6)	7.2E-5 (6.6E-5)	6.3E-3 (5.0E-5)	5.2E-2 (3.7E-5)	6.3E-2 (1.2E-4)	1.4E0 (4.2E-6)
Power-GNN	3.0E-6	5.8E-7	6.9E-7	1.3E-6	2.9E-7	3.0E-6

Task: SE & PE. Power GNN vs Vanilla NN. Experiments.



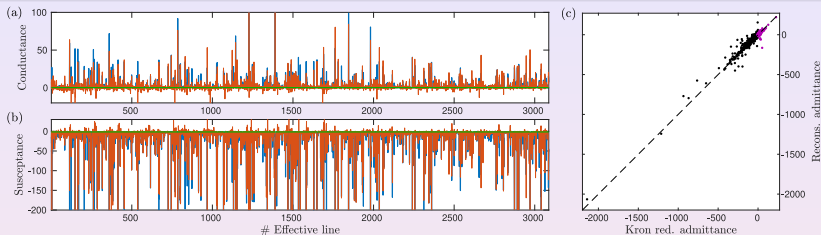
Full Observability. Parameter Estimation.

- Reconstruction of the admittance matrix Y for IEEE 14-bus (a), IEEE 118-bus (b) and PanTaGruEl (c) models
- The min, mean and max values are displayed as circles, crosses and squares respectively (for 10 realizations.)

Notice !!

- Quality of the reconstruction by Power-GNN – especially for large network

Task: SE & PE. Power GNN vs Vanilla NN. Experiments.



Partial Observability. Parameter Estimation. PanTaGruEl model

- Initial (pre-training) values – in green.
- Trained values and their Kron-reduction counterparts – red and blue respectively.
- (c) shows alternative visualization of the reference-vs-predicted values of the line conductances (purple) and susceptances (black)

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